A river flows toward the east. Because of your knowledge of physics, you head your boat 56° west of north and have a velocity of 4.0 m/s due north relative to the shore.

(a) What is the velocity of the current?

m/s

(b) What is your speed relative to the water?

m/s

Solution:

$$\begin{split} \alpha &= 56^\circ - \text{west of north angle;} \\ V_b &= 4 \frac{m}{s} - \text{velocity of the boat relative to the shore;} \\ V_c &- \text{velocity of the current;} \\ V_{b,c} &- \text{velocity of the boat relative to the water;} \\ \text{From the right triangle ABC:} \end{split}$$

$$\sin \alpha = \frac{V_b}{V_{b,c}} \Longrightarrow V_{b,c} = \frac{V_b}{\sin \alpha} = \frac{4\frac{m}{s}}{\sin 56^\circ} = 4.8\frac{m}{s}$$
$$\cos \alpha = \frac{V_c}{V_{b,c}} \Longrightarrow V_c = V_{b,c} \cos \alpha = 4.8\frac{m}{s} \cdot \cos 56^\circ = 2.7\frac{m}{s}$$
Answer: a) 4.8 $\frac{m}{s}$
b) 2.7 $\frac{m}{s}$

