

A ferry is crossing a river. The ferry is headed due north with a speed of 2.5 m/s relative to the water and the river's velocity is 3.5 m/s to the east. Find the direction in which the ferry is moving (measured from due east with counterclockwise positive)

Solution:

$V_{f,r} = 2.5 \frac{\text{m}}{\text{s}}$ – velocity of the ferry relative to the water;

$V_{\text{river}} = 3.5 \frac{\text{m}}{\text{s}}$ – velocity of the river;

α

– the angle between east direction and the direction of the ferry's motion

Formula for the relative velocity of the track:

$$\vec{V}_{f,r} = \vec{V}_{\text{ferry}} - \vec{V}_{\text{river}}$$

$$\vec{V}_{\text{ferry}} = \vec{V}_{f,r} + \vec{V}_{\text{river}}$$

From the right triangle ABC:

$$\tan \alpha = \frac{V_{f,r}}{V_{\text{river}}} \Rightarrow \alpha = \arctan\left(\frac{V_{f,r}}{V_{\text{river}}}\right) = \arctan\left(\frac{2.5 \frac{\text{m}}{\text{s}}}{3.5 \frac{\text{m}}{\text{s}}}\right) = 36^\circ$$

Answer: the angle between east direction and the direction of the ferry's motion is 36°

