

Motion of a particle is given by equation $s = (3t^3 + 7t^2 + 14t + 8) \text{ m}$ the value of acceleration of the particle at $t=1\text{s}$ is?

Solution.

$$s = (3t^3 + 7t^2 + 14t + 8) \text{ m}, t = 1 \text{ s};$$

$$a = ?$$

$$s = 3t^3 + 7t^2 + 14t + 8.$$

The velocity is the derivative of the displacement vector as a function of time:

$$v = \frac{ds}{dt} = 9t^2 + 14t + 14.$$

$$v = (9t^2 + 14t + 14) \frac{\text{m}}{\text{s}}.$$

The acceleration is the derivative of the velocity vector as a function of time:

$$a = \frac{dv}{dt} = 18t + 14.$$

$$a = (18t + 14) \frac{\text{m}}{\text{s}^2}.$$

The value of acceleration of the particle at $t = 1\text{s}$:

$$a = 18 \cdot 1 + 14 = 32.$$

$$a = 32 \frac{\text{m}}{\text{s}^2}.$$

Answer: The value of acceleration of the particle at $t = 1\text{s}$ is $a = 32 \frac{\text{m}}{\text{s}^2}$.