

Full energy of spring-mass system is  $W=W_p+W_k$ ;

$$W_p = \frac{kx^2}{2} - \text{Potential energy}$$

$$W_k = \frac{mV^2}{2} - \text{kinetic energy}$$

$x$  – displacement of mass;

$K$  – constant factor characteristic of the spring, its stiffness.

$m$  – mass;

$V$  – velocity of mass;

If equation of oscillation is  $x = A\cos(\omega t \pm \varphi)$  or  $x = A\sin(\omega t \pm \varphi)$ , we have

$$W_p = \frac{k(A\cos(\omega t \pm \varphi))^2}{2} = \frac{k}{2}A^2\cos^2(\omega t \pm \varphi)$$

$V = x'(t)$  - derivative from  $x(t)$

$$x'(t) = (A\sin(\omega t \pm \varphi))' = A \cdot \omega \cdot \cos(\omega t \pm \varphi)$$

$$W_k = \frac{mV^2}{2} = \frac{m}{2} \cdot A^2 \cdot \omega^2 \cdot \sin^2(\omega t \pm \varphi)$$

$$W = \frac{m}{2} \cdot A^2 \cdot \omega^2 \cdot \sin^2(\omega t \pm \varphi) + \frac{k}{2}A^2\cos^2(\omega t \pm \varphi)$$

Where  $\omega = \sqrt{k/m}$

