

Question #36084

Hi! Could you please explain the solution to me step by step?

At a party some balloons are filled with helium. To fill them they have used gas from a bottle with volume  $45 \text{ dm}^3$  and the pressure  $1.00 \text{ MPa}$ . The balloons are made to hold a pressure of  $150 \text{ kPa}$ . How many such balloons you can inflate if the balloons have an average volume of  $4.0 \text{ dm}^3$ ?

Solution:

Let

$$V_{\text{bottle}} = 45 \text{ L}$$

$$P_{\text{bottle}} = 1.00 \text{ MPa} = 1000 \text{ kPa}$$

$$V_{\text{balloons}} = 4 \text{ L}$$

$$P_{\text{balloons}} = 150 \text{ kPa}$$

---

$$N_{\text{balloons}} = ?$$

According to the Boyle's law (isothermal process )

$$V_{\text{bottle}} P_{\text{bottle}} = P_{\text{balloons}} V_{\text{total}} \text{ where } V_{\text{total}} \text{ is the total volume of the helium after inflating balloons}$$

Such as after inflating the balloons in bottle is the helium too

$$V_{\text{total}} = N_{\text{balloons}} V_{\text{balloons}} + V_{\text{bottle}}$$

$$V_{\text{bottle}} P_{\text{bottle}} = P_{\text{balloons}} (N_{\text{balloons}} V_{\text{balloons}} + V_{\text{bottle}})$$

$$N_{\text{balloons}} = \frac{\frac{V_{\text{bottle}} P_{\text{bottle}} - V_{\text{bottle}}}{P_{\text{balloons}}}}{V_{\text{balloons}}}$$

$$N_{\text{balloons}} = \frac{\frac{45 \cdot 1000}{150} - 45}{4} = 63.75$$

Such as the number of the balloons must be integer

**Answer: 63 balloons.**