

A 21.3 kg box rests on a table. A 16.8 kg box is placed on top of the first box, as shown. Determine the total force in N that the table exerts on the first box.

Solution:

$m_1 = 21.3 \text{ kg}$ – mass of the first box;

$m_2 = 16.8 \text{ kg}$ – mass of the second box;

N_1 – reaction force that acts on the first box;

N_2 – reaction force that acts on the second box;

$P_{2,1}$ – force that the second box exerts on the first box;

F – total force that the table exerts on the first box;

$P_{1,t}$ – force that the first box exerts on the table;

Newton's third law: When one body exerts a force on a second body, the second body simultaneously exerts a force equal in magnitude and opposite in direction to that of the first body:

$$1 \text{ box and 2 box: } \vec{N}_2 = -\vec{P}_{2,1}; |\vec{N}_2| = |\vec{P}_{2,1}| = m_2 g$$

$$1 \text{ box and table: } \vec{P}_{1,t} = -\vec{F}; |\vec{P}_{1,t}| = |F|$$

Newton's second law for the first box:

$$\vec{F} + \vec{P}_{2,1} + \vec{m}_1 g = \vec{0}$$

$$y: F - P_{2,1} - m_1 g = 0$$

$$F - m_2 g - m_1 g = 0$$

$$F = g(m_1 + m_2) = 9.8 \frac{\text{N}}{\text{kg}} \cdot (21.3 \text{ kg} + 16.8 \text{ kg}) = 373 \text{ N}$$

Answer: total force that the table exerts on the first box is 373N

