

A stone is thrown from ground level at 79 m/s. Its speed when it reaches its highest point is 60 m/s.

Find the angle, above the horizontal, of the stone's initial velocity.

Answer in units of °

Solution:

$V_0 = 79 \frac{\text{m}}{\text{s}}$ – initial velocity of the stone;

$V_1 = 60 \frac{\text{m}}{\text{s}}$ – velocity at the highest point;

α – angle, above the horizontal, of the stone's initial velocity;

During flight, acceleration of gravity is directed along the Y-axis, so the horizontal component of velocity does not change. horizontal component from the right triangle ABC:

$$\Delta ABC: \cos \alpha = \frac{V_x}{V_0}$$

$$V_x = V_0 \cdot \cos \alpha \quad (1)$$

When the stone is located at the top of the trajectory (highest point), the vertical component of the velocity is zero, then all speed - is the horizontal component.

$$V_1 = V_x \quad (2)$$

(2)in(1):

$$V_1 = V_0 \cdot \cos \alpha$$

$$\cos \alpha = \frac{V_1}{V_0}$$

$$\alpha = \arccos\left(\frac{V_1}{V_0}\right) = \arccos\left(\frac{60 \frac{\text{m}}{\text{s}}}{79 \frac{\text{m}}{\text{s}}}\right) = 41^\circ$$

Answer: angle, above the horizontal, of the stone's initial velocity is 41°.

