

The ranges of the bullets fired from a gun at angle θ , 2θ and 4θ are found in the ratio $x : 2 : 2$, then the value of x will be (Assume same speed of bullets)

- A) 1
- B) 2
- C) $\sqrt{3}$
- D) none of these.

The total horizontal distance travelled by the projectile equals:

$$d = \frac{v^2 \sin(2\alpha)}{g}$$

g - the gravitational acceleration

α - the angle at which the projectile is launched

v - the velocity at which the projectile is launched

If ratio of the ranges of the bullets fired from a gun at 2θ and 4θ is found in the ratio $2 : 2$, then:

$$\sin 4\theta = \sin 8\theta \Rightarrow \theta = 15^\circ \quad (\sin 60^\circ = \sin 120^\circ = \frac{\sqrt{3}}{2})$$

Range of the bullet fired from a gun at angle θ equals:

$$d = \frac{v^2 \sin(2\theta)}{g} = \frac{v^2 \sin(30^\circ)}{g} = \frac{v^2}{2g}$$

Range of the bullet fired from a gun at angle 2θ equals:

$$d = \frac{v^2 \sin(4\theta)}{g} = \frac{v^2 \sin(60^\circ)}{g} = \frac{\sqrt{3}v^2}{2g}$$

Ratio of the ranges equals:

$$1 : \sqrt{3} \text{ or } \frac{2}{\sqrt{3}} : 2$$

Answer: D) none of these.