

Question 32368

One needs to use the laws of conservation of linear momentum and energy. First one gives:

$$1) m_e v = m_e v' + M_H v''$$

, where m_e is the mass of electron, v is the initial electron velocity, v' is the final electron velocity, M_H is the mass of hydrogen atom and v'' is the velocity of Hydrogen atom after collision. Also, $\frac{M_H}{m_e} = 1837$ (according to given conditions).

Law of conservation of energy gives:

$$2) m_e v^2 = m_e v'^2 + M_H v''^2 .$$

$$\text{From equation 1), obtain } v' = v - \frac{M_H}{m_e} v'' .$$

Plugging latter expression into 2):

$$m_e v^2 = m_e \left(v - \frac{M_H}{m_e} v'' \right)^2 + M_H v''^2 .$$

Opening brackets in latter expression, obtain $0 = -2v v'' M_H + \frac{M_H^2}{m_e} v''^2 + M_H v''^2$. Dividing by

$$m_e v'' , \text{ get } 2v \frac{M_H}{m_e} = v'' \left(\frac{M_H^2}{m_e^2} + \frac{M_H}{m_e} \right) , \text{ from which obtain connection between } v'' \text{ and } v$$

$$(\text{using } \frac{M_H}{m_e} = 1837) : v'' = \frac{2 \cdot 1837}{(1837^2 + 1837)} v = 1.09 \cdot 10^{-3} v .$$

The ratio of kinetic energy of the hydrogen atom after the collision to that of the electron before the collision is:

$$k = \frac{\frac{M_H v''^2}{2}}{\frac{m_e v^2}{2}} = \frac{M_H v''^2}{m_e v^2} = 1837 \cdot (1.09 \cdot 10^{-3})^2 = 0.0022 .$$