

Task. Assuming zero friction, what is the initial velocity of a projectile that is fired straight up from the ground and takes 8 seconds to hit the ground.

Solution. We should find the initial velocity v_0 of the projectile.

Notice that the projectile moved with constant acceleration $g = 9.8 \text{ m/s}^2$, and so the height of the projectile at time t is given by the formula

$$h(t) = v_0 t - \frac{gt^2}{2}.$$

By assumption the projectile hit the ground after 8 seconds, that is $h(8) = 0$. Hence we get the following equation

$$0 = h(8) = v_0 * 8 - \frac{g * 8^2}{2} \quad \Rightarrow \quad 8v_0 = \frac{64g}{2} = 32g,$$

and so

$$v_0 = 4g = 4 * 9.8 = 39.2 \text{ m/s}.$$

Answer. 39.2 m/s.