

### Question 23382

1. Let  $oy$  axis has the same direction as  $\vec{g}$ . Then, y component of velocity

$$v_y(t) = v_0 + g t, \text{ where } v_0 = 70 \frac{ft}{s} = 70 \cdot 0.3 \frac{m}{s} = 21 \frac{m}{s} \text{ and } g = 10 \frac{m}{s^2}. \text{ Integrating}$$

formula for y component of velocity, obtain:  $y(t) = -h + v_0 t + \frac{g t^2}{2}$ ,  $h = 50 \text{ ft} = 15 \text{ m}$ . For

moment when stone stops:  $0 = -h + v_0 t + \frac{g t^2}{2}$ ;  $-15 + 21 t + 5 t^2 = 0 \Rightarrow t \approx 0.62 \text{ s}$ . Hence,

velocity at this moment is  $v_y = 21 \frac{m}{s} + 10 \cdot 0.62 = 27.2 \frac{m}{s}$ .

2. Let  $oy$  axis be vertically up.

Then, equations of motion are:  $v_x(t) = v$ ;  $v_y(t) = -g t$ ,  $x(t) = v t$ ;  $y(t) = h - \frac{g t^2}{2}$ .

Let  $t_1$  be the moment when water strikes the ground. For this moment,

$$h = \frac{g t_1^2}{2} \Rightarrow t_1 = \sqrt{2 \frac{h}{g}}, \text{ when for x-component of motion } 4 = v t_1 \Rightarrow v = \frac{4}{t_1} = \sqrt{8 \frac{g}{h}} \approx 7.3 \frac{m}{s}.$$

Speed, when water strikes the ground is  $v = \sqrt{v_x^2 + v_y^2}|_{t=t_1} = \sqrt{v^2 + 2 g h} = 9.13 \frac{m}{s}$ . Initial

speed is  $v = 7.3 \frac{m}{s}$ .