

## Question 23382

1. Let  $oy$  axis has the same direction as  $\vec{g}$ . Then, y component of velocity  $v_y(t) = v_0 + gt$ , where  $v_0 = 70 \frac{ft}{s} = 70 \cdot 0.3 \frac{m}{s} = 21 \frac{m}{s}$  and  $g = 10 \frac{m}{s^2}$ . Integrating formula for y component of velocity, obtain:  $y(t) = -h + v_0 t + \frac{gt^2}{2}$ ,  $h = 50 \text{ ft} = 15 \text{ m}$ . For moment when stone stops:  $0 = -h + v_0 t + \frac{gt^2}{2}$ ;  $-15 + 21t + 5t^2 = 0 \Rightarrow t \approx 0.62 \text{ s}$ . Hence, velocity at this moment is  $v_y = 21 \frac{m}{s} + 10 \cdot 0.62 = 27.2 \frac{m}{s}$ .

2. Let  $oy$  axis be vertically up.

Then, equations of motion are:  $v_x(t) = v$ ;  $v_y(t) = -gt$ ,  $x(t) = vt$ ;  $y(t) = h - \frac{gt^2}{2}$ .

Let  $t_1$  be the moment when water strikes the ground. For this moment,

$$h = \frac{gt_1^2}{2} \Rightarrow t_1 = \sqrt{2 \frac{h}{g}}$$
, when for x-component of motion  $4 = vt_1 \Rightarrow v = \frac{4}{t_1} = \sqrt{8 \frac{g}{h}} \approx 7.3 \frac{m}{s}$ .

Speed, when water strikes the ground is  $v = \sqrt{v_x^2 + v_y^2} \Big|_{t=t_1} = \sqrt{v^2 + 2gh} = 9.13 \frac{m}{s}$ . Initial speed is  $v = 7.3 \frac{m}{s}$ .