

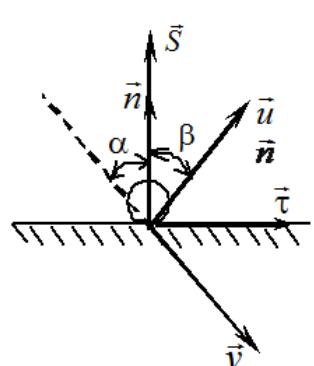
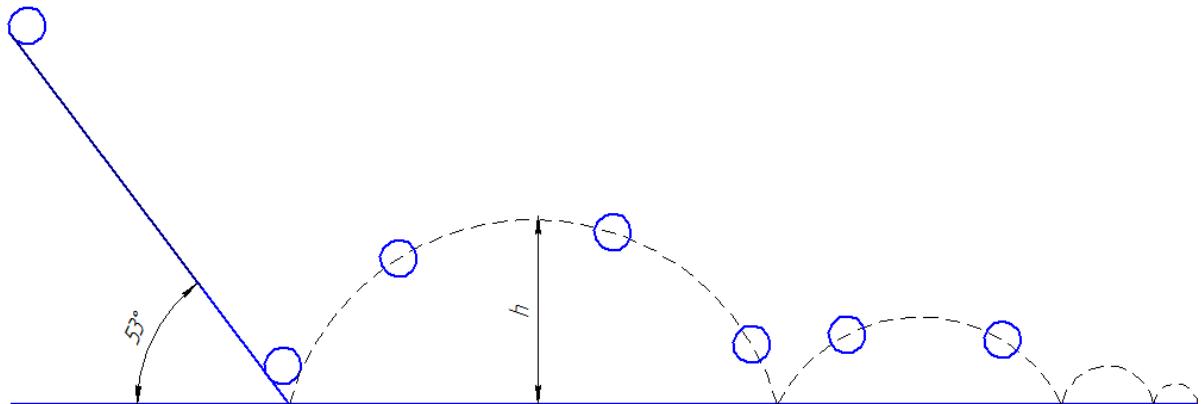
Task:

A ball is released from rest at a height of 10m on an inclined plane of inclination 53 degrees. If coefficient of restitution for collision is 3/4. Then its total time of motion is approximately...

a) 3.5 sec b) 8.6 sec c) 12.8 sec d) 22 sec

what is the exact process of doing this question???

Solution:



$$mu_n - mv_n = S$$

$$mu_\tau - mv_\tau = 0$$

$$k = \frac{|u_n|}{|v_n|}$$

$$k = \frac{\tan \alpha}{\tan \beta}$$

$$u_n = u \cos \beta$$

$$u_\tau = u \sin \beta$$

$$v_n = -v \cos \alpha$$

$$v_\tau = v \sin \alpha$$

$$u = v \sqrt{\sin^2 \alpha + k^2 \cos^2 \alpha}$$

$$S = m(k+1)v \cos \alpha$$

$$k = \frac{3}{4}$$

$$\alpha = 90^\circ - 53^\circ = 37^\circ$$

$$\tan \beta = \frac{\tan 37^\circ}{\frac{3}{4}}, \beta = \arctan \frac{\tan 37^\circ}{\frac{3}{4}} = 45.1354^\circ$$

$$10 \text{ m} = \frac{g \cdot t_{inc}^2}{2}$$

$$t_{inc} = \sqrt{\frac{2 \cdot 10m}{g}} = 1.4278 \text{ s}$$

$$10 \text{ m} = \frac{v_n^2}{2g}$$

$$v_n = \sqrt{2 \cdot g \cdot 10m} = 14.0071 \frac{m}{s}$$

$$h = \frac{u_n^2}{2g} = u_n \cdot \frac{t}{2} - g \cdot \frac{\left(\frac{t}{2}\right)^2}{2}$$

$$\frac{u_n^2}{g} = u_n \cdot t - g \cdot \left(\frac{t}{2}\right)^2$$

$$t = \frac{2 \cdot u_n}{g} - \text{the time of flying up and down}$$

$$t_{total} = t_{inc} + \sum_{i=1}^{\infty} \frac{2 \cdot u_{n_i}}{g} = t_{inc} + \frac{2}{g} \sum_{i=1}^{\infty} u_{n_i}$$

$$u_{n_i} = k \cdot u_{n_{i-1}}$$

$$u_{n_i} = u_{n_1} \cdot k^{i-1} = v_n \cdot k^{i-1}$$

$$t_{total} = t_{inc} + \frac{2}{g} \sum_{i=1}^{\infty} v_n \cdot k^{i-1} = t_{inc} + \frac{2}{g} \cdot \frac{v_n}{1-k} = 1.4278 \text{ s} + \frac{2}{9.81 \frac{m}{s^2}} \cdot \frac{14.0071 \frac{m}{s}}{1 - \frac{3}{4}} = 12.8 \text{ s}$$

Answer:

$$t_{total} = 12.8 \text{ s}$$