

Question#20151

a steel ball bearing is 4cm at 20c.a bronze plate has a hole in it that is 3.9cm in diameter at 20c.what common temperature must they have so the ball just spueezs through the hole ?.

Solution:

Let:

$$D_1 = 4 \text{ cm}$$

$$D_2 = 3.9 \text{ cm}$$

$$t_0 = 20 \text{ }^\circ\text{C}$$

t - ?

$$D_1^t = D_1 + D_1 \alpha_{\text{steel}} (t_1 - t_0)$$

$$D_2^t = D_2 + D_2 \alpha_{\text{bronze}} (t_1 - t_0)$$

Were:

$$\alpha_{\text{steel}} = 11 * 10^{-6} \text{ }^\circ\text{C}^{-1} \quad \text{Is the coefficient of thermal expansion of the steel.}$$

$$\alpha_{\text{bronze}} = 18 * 10^{-6} \text{ }^\circ\text{C}^{-1} \quad \text{Is the coefficient of thermal expansion of the bronze.}$$

Such as:

$$D_1^t = D_2^t$$

$$D_1 + D_1 \alpha_{\text{steel}} (t - t_0) = D_2 + D_2 \alpha_{\text{bronze}} (t - t_0)$$

$$t = \frac{D_1(t_0 \alpha_{\text{steel}} - 1) - D_2(t_0 \alpha_{\text{bronze}} - 1)}{D_1 \alpha_{\text{steel}} - D_2 \alpha_{\text{bronze}}}$$

$$t = \frac{4(20 * 11 * 10^{-6} - 1) - 3.9(20 * 18 * 10^{-6} - 1)}{4 * 11 * 10^{-6} - 3.9 * 18 * 10^{-6}} = 3837 \text{ }^\circ\text{C}$$

Answer: 3837 °C.