

**Problem:**

Starting at rest  $t=0$ , a wheel undergoes a constant angular acceleration. When  $t=2.33\text{sec}$ , the angular velocity of a wheel is  $4.96\text{rad/s}$ . The acceleration continues until  $t=23.0\text{s}$ , when it abruptly ceases. Through what angle does the wheel rotate in the interval  $t=0$  to  $t=46.0\text{s}$ ?

**Solution:**

According to kinematics of angular movement:

$$\beta = \frac{\omega_1}{t_1} = \frac{4.96}{2.33} = 2.13 \left[ \frac{\text{rad}}{\text{s}^2} \right]$$

$$\omega_2 = \beta t_2 = \omega_1 \frac{t_2}{t_1} = 4.96 * \frac{23}{2.33} = 49 \text{ [rad/s]}$$

$$\begin{aligned} \varphi &= \varphi_{t_2} + \omega_2(t_3 - t_2) = \frac{\beta t_2^2}{2} + \omega_2(t_3 - t_2) = \frac{\omega_1}{t_1} * \frac{t_2^2}{2} + \omega_2(t_3 - t_2) \\ &= 2.13 * \frac{23^2}{2} + 49 * (46 - 23) = 1690 \text{ [rad]} \end{aligned}$$

Where  $\beta$  – angular acceleration;

$\omega_1 = 4.96 \text{ rad/s}$  – angular speed at time  $t_1 = 2.33 \text{ s}$ ;

$\omega_2$  – angular speed at time  $t_2 = 23 \text{ s}$ ;

$t_3 = 46 \text{ s}$  – stop time;

$\varphi$  – whole angle, that wheel rotate through time  $t_3$ ;

$\varphi_{t_2}$  – angle, that wheel rotate through time  $t_2$ ;

**Answer:**  $\varphi = 1690 \text{ [rad]}$ .