

Komal likes to have a tepid bath. She has 5 kg of water at 25 (degree Celcius). How many kg of water should she boil to have a comfortable bath of 45 (degree Celcius)?

Solution:

Let:

$$m_1 = 5 \text{ kg}$$

$$T_1 = 25^\circ\text{C}$$

$$T_2 = 100^\circ\text{C} \text{ the temperature of boiling water}$$

$$T_3 = 45^\circ\text{C}$$

$$m_2 = ?$$

According to the laws of thermodynamics:

$$Q_1 + Q_2 = Q_3$$

$$m_1 c T_1 + m_2 c T_2 = (m_1 + m_2) c T_3$$

$$m_1 T_1 + m_2 T_2 = m_1 T_3 + m_2 T_3$$

$$m_2 (T_2 - T_3) = m_1 T_3 - m_1 T_1$$

$$m_2 = \frac{m_1 T_3 - m_1 T_1}{T_2 - T_3}$$

$$m_2 = \frac{5 \cdot 45 - 5 \cdot 25}{100 - 45} = 1.82 \text{ kg}$$

Answer: 1.82 kg