Problem:

3 thin uniform rods each of length L & amp; mass M are joined to form an equilateral triangle .find the moment of inertia of the system about an axis along 1 side of the triangle?

Solution:

According to the definition of momentum of inertia:



$$I = \sum_{i} m_{i} r_{i}^{2}$$

In this case:

$$I = 2 * \int_{0}^{L\frac{\sqrt{3}}{2}} r^{2} dm = \int_{0}^{L\frac{\sqrt{3}}{2}} r^{2} \frac{M}{L} dl = \int_{0}^{L\frac{\sqrt{3}}{2}} r^{2} \frac{M}{L} \frac{dr}{\cos\frac{\pi}{6}} = \frac{2M}{\sqrt{3}L} \int_{0}^{L\frac{\sqrt{3}}{2}} r^{2} dr$$
$$= \frac{1}{2}ML^{2}$$

Here integral gives the momentum of inertia of only one rod. Thus, it is multiplied by 2.

Answer:
$$I = \frac{1}{2}ML^2$$
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