



Suppose the particle has coordinates (R, ϕ) at some moment t . The formula for radial acceleration is:

$$a = \frac{v^2}{R}$$

where v is a tangential velocity.

As v is perpendicular to OB (because it is tangential velocity), we get from the scheme that:

$$v = u \sin \phi$$

Then

$$a(R, \phi) = \frac{u^2 \sin^2 \phi}{R}$$

If we assume that at the moment $t_0 = 0$ the particle was at the point A (just in opposite to the origin), then it was at the point B at some moment t and $AB = ut$.

Then we get:

$$R = \sqrt{u^2 t^2 + d^2}$$

and

$$\tan \phi = \frac{d}{ut}$$

$$\text{So, } \sin^2 \phi = 1 - \cos^2 \phi = 1 - \frac{1}{1 + \tan^2 \phi} = \frac{\tan^2 \phi}{1 + \tan^2 \phi} = \frac{d^2}{u^2 t^2 + d^2}.$$

Finally,

$$a(t) = \frac{u^2}{\sqrt{u^2 t^2 + d^2}} * \frac{d^2}{u^2 t^2 + d^2} = \frac{u^2 d^2}{(u^2 t^2 + d^2)^{\frac{3}{2}}}$$