

An ant lives on the surface of a cube with edges of length 7cm. It is currently located on an edge x cm from one of its ends. While traveling on the surface of the cube, it has to reach the grain located on the opposite edge (also at a distance x cm from one of its ends) as shown below.

(i) What is the length of the shortest route to the grain if $x = 2$ cm? How many routes of this length are there?

The shortest way is

$$S = (7 - x) + 7 + 7 + x = 21 \text{ cm.}$$

There are two such ways.

(ii) Find an x for which there are four distinct shortest length routes to the grain.

For $x = 3.5$ cm there are 4 such ways.