

$\sin\theta = \frac{2}{55}$  and  $\cos\varphi = -\frac{2}{5}$  and  $\theta$  and  $\varphi$  lies in the second quadrant.

1. Determine  $\cos\theta$ ?

$$\cos^2\theta + \sin^2\theta = 1$$

$$\cos\theta = \pm\sqrt{1 - \sin^2\theta}$$

If  $\theta$  lie in the second quadrant than  $\cos\theta < 0$

$$\cos\theta = -\sqrt{1 - \left(\frac{2}{55}\right)^2} = -\sqrt{1 - \frac{4}{3025}} = -\frac{\sqrt{3021}}{55}$$

2. Find  $\sin\varphi$

$$\cos^2\varphi + \sin^2\varphi = 1$$

$$\sin\varphi = \pm\sqrt{1 - \cos^2\varphi}$$

If  $\varphi$  lie in the second quadrant than  $\sin\varphi > 0$

$$\sin\varphi = \sqrt{1 - \cos^2\varphi} = \sqrt{1 - \left(-\frac{2}{5}\right)^2} = \sqrt{\frac{21}{25}} = \frac{\sqrt{21}}{5}$$

3. What  $\sin(\varphi + \theta)$ ?

$$\sin(\varphi + \theta) = \sin\varphi\cos\theta + \cos\varphi\sin\theta$$

$$\sin(\varphi + \theta) = \frac{\sqrt{21}}{5} \left(-\frac{\sqrt{3021}}{55}\right) + \left(-\frac{2}{5}\right) \frac{2}{55} = -\frac{3\sqrt{7049} + 4}{275}$$

4. Find  $\cos(\varphi + \theta)$ ?

$$\cos(\varphi + \theta) = \left(-\frac{2}{5}\right) \left(-\frac{\sqrt{3021}}{55}\right) - \frac{\sqrt{21}}{5} \frac{2}{55} = \frac{2\sqrt{3021} - 2\sqrt{21}}{275}$$

5. Determine  $\text{tg}(\theta - \varphi)$

$$\text{tg}(\theta - \varphi) = \frac{\text{tg}\theta + \text{tg}\varphi}{1 - \text{tg}\theta\text{tg}\varphi}$$

$$\operatorname{tg}\theta = \frac{\sin\theta}{\cos\theta} = \frac{\frac{2}{55}}{-\frac{\sqrt{3021}}{55}} = -\frac{2}{\sqrt{3021}}$$

$$\operatorname{tg}\varphi = \frac{\sin\varphi}{\cos\varphi} = \frac{\frac{\sqrt{21}}{5}}{-\frac{2}{5}} = -\frac{\sqrt{21}}{2}$$

$$\operatorname{tg}(\theta - \varphi) = \frac{-\frac{2}{\sqrt{3021}} + -\frac{\sqrt{21}}{2}}{1 - \frac{2}{\sqrt{3021}} * \frac{\sqrt{21}}{2}} = \frac{-4 - \sqrt{63441}}{2\sqrt{3021} - 2\sqrt{21}}$$

6. Equivalent to  $\sin(\theta - \varphi)$ ?

$$\sin(\theta - \varphi) = \sin\theta\cos\varphi - \cos\theta\sin\varphi$$

$$\sin(\theta - \varphi) = \frac{2}{55} \left(-\frac{2}{5}\right) + \frac{\sqrt{3021}}{55} \frac{\sqrt{21}}{5} = \frac{-4 + 3\sqrt{7049}}{275}$$