

Answer to Question #91025 – Math – Calculus

Question

Find the rate of change of $h(x) = 2 \cos[(3x + \tan x)]$ with respect to x .

Solution

We know that, rate of change of a function with respect to (w.r.t.) x is same as differentiating it w.r.t x .

$$h(x) = 2 \cos(3x + \tan x)$$

On differentiating both sides w.r.t. x ,

$$h'(x) = 2[-\sin(3x + \tan x)] \times \frac{d(3x + \tan x)}{dx} \quad [\text{Using chain rule}]$$

$$h'(x) = 2[-\sin(3x + \tan x)] \times (3 + \sec^2 x) \quad \left[\because \frac{d(\tan x)}{dx} = \sec^2 x \right]$$

$$h'(x) = -2(3 + \sec^2 x) \sin(3x + \tan x).$$