## Answer on Question \#84330 - Math - Other

## Question

A sales manager wishes to assign four sales territories to four salespersons. The salespersons differ in their ability and skills and consequently the sales expected in each territory are different. The estimates of sales per month for each salesperson in different territories are given below:

|  |  | Estimated monthly sales territory |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 1 | 2 | 3 | 4 |
|  | A | 20 | 40 | 45 | 30 |
|  | B | 50 | 40 | 55 | 40 |
|  | C | 45 | 40 | 42 | 50 |
|  | D | 48 | 50 | 42 | 45 |

Find the optimal assignment of the four salespersons to the four different territories and the maximum monthly sales.

## Solution

The problem can be solved by complete enumeration method:

| No. | Assignment | Sales | No. | Assignment | Sales |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $1 \mathrm{~A}, 2 \mathrm{~B}, 3 \mathrm{C}, 4 \mathrm{D}$ | 147 | 13 | $3 \mathrm{~A}, 1 \mathrm{~B}, 2 \mathrm{C}, 4 \mathrm{D}$ | 180 |
| 2 | $1 \mathrm{~A}, 2 \mathrm{~B}, 4 \mathrm{C}, 3 \mathrm{D}$ | 152 | 14 | $3 \mathrm{~A}, 1 \mathrm{~B}, 4 \mathrm{C}, 2 \mathrm{D}$ | 195 |
| 3 | $1 \mathrm{~A}, 3 \mathrm{~B}, 2 \mathrm{C}, 4 \mathrm{D}$ | 160 | 15 | $3 \mathrm{~A}, 2 \mathrm{~B}, 1 \mathrm{C}, 4 \mathrm{D}$ | 175 |
| 4 | $1 \mathrm{~A}, 3 \mathrm{~B}, 4 \mathrm{C}, 2 \mathrm{D}$ | 175 | 16 | $3 \mathrm{~A}, 2 \mathrm{~B}, 4 \mathrm{C}, 1 \mathrm{D}$ | 183 |
| 5 | $1 \mathrm{~A}, 4 \mathrm{~B}, 2 \mathrm{C}, 3 \mathrm{D}$ | 142 | 17 | $3 \mathrm{~A}, 4 \mathrm{~B}, 1 \mathrm{C}, 2 \mathrm{D}$ | 180 |
| 6 | $1 \mathrm{~A}, 4 \mathrm{~B}, 3 \mathrm{C}, 2 \mathrm{D}$ | 152 | 18 | $3 \mathrm{~A}, 4 \mathrm{~B}, 2 \mathrm{C}, 1 \mathrm{D}$ | 173 |
| 7 | $2 \mathrm{~A}, 1 \mathrm{~B}, 3 \mathrm{C}, 4 \mathrm{D}$ | 177 | 19 | $4 \mathrm{~A}, 1 \mathrm{~B}, 2 \mathrm{C}, 3 \mathrm{D}$ | 162 |
| 8 | $2 \mathrm{~A}, 1 \mathrm{~B}, 4 \mathrm{C}, 3 \mathrm{D}$ | 182 | 20 | $4 \mathrm{~A}, 1 \mathrm{~B}, 3 \mathrm{C}, 2 \mathrm{D}$ | 172 |
| 9 | $2 \mathrm{~A}, 3 \mathrm{~B}, 1 \mathrm{C}, 4 \mathrm{D}$ | 185 | 21 | $4 \mathrm{~A}, 2 \mathrm{~B}, 1 \mathrm{C}, 3 \mathrm{D}$ | 157 |
| 10 | $2 \mathrm{~A}, 3 \mathrm{~B}, 4 \mathrm{C}, 1 \mathrm{D}$ | 193 | 22 | $4 \mathrm{~A}, 2 \mathrm{~B}, 3 \mathrm{C}, 1 \mathrm{D}$ | 160 |
| 11 | $2 \mathrm{~A}, 4 \mathrm{~B}, 1 \mathrm{C}, 3 \mathrm{D}$ | 167 | 23 | $4 \mathrm{~A}, 3 \mathrm{~B}, 1 \mathrm{C}, 2 \mathrm{D}$ | 180 |
| 12 | $2 \mathrm{~A}, 4 \mathrm{~B}, 3 \mathrm{C}, 1 \mathrm{D}$ | 170 | 24 | $4 \mathrm{~A}, 3 \mathrm{~B}, 2 \mathrm{C}, 1 \mathrm{D}$ | 173 |

Answer: The optimal assignment is $3 \mathrm{~A}, 1 \mathrm{~B}, 4 \mathrm{C}, 2 \mathrm{D}$; the maximum monthly sales are 195.

