

## Answer on Question #83982 – Math – Analytic Geometry

### Question

Equation of one side of a square is  $2x + 3y + 4 = 0$ . If the center is  $(1, 1)$  then find the equations of adjoined two sides of the square.

### Solution

The distance from the center to the given side is  $h = \frac{|ax_0 + by_0 + c|}{\sqrt{a^2 + b^2}} = \frac{|2 \cdot 1 + 3 \cdot 1 + 4|}{\sqrt{2^2 + 3^2}} = \frac{9}{\sqrt{13}}$ .

The center point doesn't lie on the side because  $h \neq 0$ .

The equation of the line through the point perpendicular to given side is  $0 \equiv bx - ay - bx_0 + ay_0 := bx - ay + c_0 = 3x - 2y - 1$ .

The equations of adjoined two sides are  $bx - ay + c_0 \pm h\sqrt{b^2 + (-a)^2} = 0$ , i.e.  $3x - 2y + 8 = 0$  and  $3x - 2y - 10 = 0$ .

### Answer:

$$3x - 2y + 8 = 0, 3x - 2y - 10 = 0.$$