Answer to Question #83791 - Math - Algebra

Question

 $6x^3 - 48x^2 + x - 8$ Simplify it.

Solution

$$6x^3 - 48x^2 + x - 8 = 0$$
(1)

Assume x = 8, put in equation (1) and get the correct equality

$$6 * 8^3 - 48 * 8^2 + 8 - 8 = 0$$

It means that x = 8 is a solution of the equation (1),

dividing the left-hand side of the equation (1) by x - 8

$$\frac{6x^3 - 48x^2 + x - 8}{x - 8} = 6x^2 + 1$$

Thus, we can rewrite

$$6x^3 - 48x^2 + x - 8 = (6x^2 + 1)(x - 8) = 0$$

So
$$(x - 8) = 0$$
 or $(6x^2 + 1) = 0$

From (x - 8) = 0 it follows that x = 8

From $(6x^2 + 1) = 0$ it follows that $x^2 = -\frac{1}{6}$, $x = \pm \frac{i}{\sqrt{6}}$.

Answer: x = 8, $x = +\frac{i}{\sqrt{6}}$, $x = -\frac{i}{\sqrt{6}}$.