

ANSWER TO QUESTION NO #83626 – MATH – ALGEBRA

QUESTION

What is the point-slope equation for $y = 2x + 3$

ANSWER

DEFINITION OF POINT-SLOPE FORM:

It is line geometry function mathematically defined by the formula $y - y_1 = m(x - x_1)$. It illustrates that the difference between the two points ($y - y_1$) of 'y' coordinate on a line is proportional to the difference between the two points ($x - x_1$) of 'x' coordinate on a line.

'm' is the slope of a line

(x₁, y₁) is any point on a line

FORMULA: The formula which is used to find the point-slope form of a line

$$(y - y_1) = m(x - x_1)$$

'm' is the slope of a line

(x₁, y₁) is any point on a line

SOLUTION

In this question the equation of the line is $y = 2x + 3$

'm' = 2, the slope of the line

So, for this question the equation can be written in this form,

$$y = 2x + 4 - 1$$

$$y = 2(x + 2) - 1$$

$$y + 1 = 2(x + 2)$$

$$y - (-1) = 2(x + 2)$$

So, a point – slope form of this equation can be written as $y - (-1) = 2(x + 2)$

The point-slope form of this equation can be written in this way also-

$$y = 2x + 3$$

$$y = 2\left(x + \frac{3}{2}\right)$$

$$y - 0 = 2\left(x - \left(-\frac{3}{2}\right)\right)$$

Thus, for different coordinates different point-slope form can be formed. Two point-slope forms which I am producing here are

$$y - (-1) = 2(x - (-2)) \text{ (ANSWER)}$$

$$y - 0 = 2\left(x - \left(-\frac{3}{2}\right)\right) \text{ (ANSWER)}$$

For the first point-slope form coordinate on the line is, (-2,-1)

2nd point-slope form coordinate on the line is, (-3/2,0)

Try to evaluate other point-slope form which can be formed for different coordinates on the line.

Another point-slope form which can be formed is

$$y = 2x + 3$$

$$y = 2x + 6 - 3$$

$$y - (-3) = 2(x - (-3)) \text{ (ANSWER)}$$