

Answer on Question #83568 – Math – Trigonometry

Question

$$\tan\theta = \sqrt{15}/15$$

$$\sin(-\theta) = -1/4$$

What is the value of $\cos(\theta)$?

$$-\frac{\sqrt{15}}{60}$$

$$-\frac{\sqrt{15}}{4}$$

$$\frac{\sqrt{15}}{60}$$

$$\frac{\sqrt{15}}{4}$$

Answer

INSTRUCTIONS:

$$\sin(-\theta) = -\sin\theta$$

$$-\sin\theta = -\frac{1}{4}$$

$$\sin\theta = 1/4$$

FORMULA:

$$\sin^2\theta + \cos^2\theta = 1$$

$$\tan\theta = \frac{\sin\theta}{\cos\theta}$$

SOLUTION:

$$\cos\theta = \pm\sqrt{1 - \sin^2\theta}$$

$$\cos\theta = \pm \sqrt{1 - \left(\frac{1}{16}\right)}$$

$$\cos\theta = \pm \frac{\sqrt{15}}{4}$$

NOW, $\sin\theta = 1/4$, if, $\cos\theta = -\sqrt{15}/4$, $\tan\theta = \frac{\sin\theta}{\cos\theta} = \frac{\frac{1}{4}}{\frac{-\sqrt{15}}{4}} = -\sqrt{15}/15$, which is not given in the problem...

SO, $\cos\theta = \sqrt{15}/4$,

$$\sin\theta = 1/4$$

$$\tan\theta = \frac{\frac{1}{4}}{\frac{\sqrt{15}}{4}} = \frac{1}{\sqrt{15}} = \frac{\sqrt{15}}{\sqrt{15} * \sqrt{15}} = \frac{\sqrt{15}}{15} \text{ (cross checking with the problem)}$$

SO, our answer is $\cos\theta = \frac{\sqrt{15}}{4}$.

Answer: $\cos\theta = \frac{\sqrt{15}}{4}$.