

## Answer on Question #83340 – Math – Statistics and Probability

### Question

Given that  $Y \sim b(y; 4, 0.4)$ , find the probabilities of the following events:

(a)  $P(Y < 2)$

(b)  $P(Y = 2)$

(c)  $P(Y > 2)$

### Solution

(a)  $P(Y < 2)$ :

$$P(Y < 2) = Y \sim b(0; 4, 0.4) + Y \sim b(1; 4, 0.4) = \frac{4!}{0!(4-0)!} 0.4^0 (1 - 0.4)^{4-0} + \\ + \frac{4!}{1!(4-1)!} 0.4^1 (1 - 0.4)^{4-1} = 0.1296 + 0.3456 = 0.4752$$

(b)  $P(Y = 2)$ :

$$P(Y = 2) = Y \sim b(2; 4, 0.4) = \frac{4!}{2!(4-2)!} 0.4^2 (1 - 0.4)^{4-2} = 0.3456$$

(c)  $P(Y > 2)$

$$P(Y > 2) = Y \sim b(3; 4, 0.4) + Y \sim b(4; 4, 0.4) = \frac{4!}{3!(4-3)!} 0.4^3 (1 - 0.4)^{4-3} + \\ + \frac{4!}{4!(4-4)!} 0.4^4 (1 - 0.4)^{4-4} = 0.1536 + 0.0256 = 0.1792$$

**Answer:**

(a)  $P(Y < 2) = 0.4752$ ;

(b)  $P(Y = 2) = 0.3456$ ;

(c)  $P(Y > 2) = 0.1792$ .