## Answer on Question \#82894 - Math - Analytic Geometry

## Question

A line $A B$ passes through the point $P(3,-2)$ with gradient 2 , determine the equation of the line CD through $P$ perpendicular to AB.

## Solution

If gradient (slope) of line $A B$ is $m=2$, then gradient of the line $C D$ perpendicular to $A B$ is

$$
m_{1}=-\frac{1}{m}=-\frac{1}{2}
$$

So, the equation of the line CD:

$$
\begin{aligned}
& y=m_{1} x+b \\
& y=-\frac{1}{2} x+b
\end{aligned}
$$

Substitute the coordinates of the point $P$ which lies in the line CD:

$$
\begin{gathered}
-2=-\frac{1}{2} \cdot 3+b \\
b=-\frac{1}{2}
\end{gathered}
$$

Thus, the equation of the line $C D$ is

$$
y=-\frac{1}{2} x-\frac{1}{2}
$$

Answer: $y=-\frac{1}{2} x-\frac{1}{2}$.

