

Answer on Question #81793 – Math – Statistics and Probability

Question

In an experiment, A and B are events with probabilities $P[A] = 5/8$ and $P[B] = 3/8$. Furthermore, A and B are independent. Find $P[A \cup B]$.

1. $1/8$
2. $3/8$
3. $7/8$
4. $9/64$
5. $15/64$
6. $25/64$
7. $49/64$
8. $55/64$
9. impossible to determine based on the given information.

Solution

Apply the inclusion-exclusion principle:

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

Since A and B are independent, $P(A \cap B) = P(A)P(B)$. Then

$$P(A \cup B) = P(A) + P(B) - P(A)P(B) = \frac{5}{8} + \frac{3}{8} - \frac{5}{8} \cdot \frac{3}{8} = \frac{49}{64}$$

Answer: option 7. $49/64$ is correct.