## Answer on Question \#81193 - Math - Statistics and Probability

## Question

For the following data

| $\mathbf{x}$ | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{f}$ | 1 | 9 | 26 | 59 | 72 | 52 | 29 | 7 | 1 |

Calculate the quartiles $Q_{1}, Q_{2}$, and $Q_{3}$.

## Solution

There is no common definition of quartiles and they can be selected in different ways. The Wikipedia article describes 3 methods to split off a set of data into four equal groups (quarters). First of all, the values must be sorted in ascending order (by finding the next larger value):

| $\mathbf{f}$ | 1 | 9 | 26 | 59 | 72 | 52 | 29 | 7 | 1 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 |  |  |  |  |  |  |  |  |
|  | 1 | 1 |  |  |  |  |  |  |  |
|  | 1 | 1 | 7 |  |  |  |  |  |  |
| $\mathbf{S}$ | 1 | 1 | 7 | 9 | 26 | 29 | 52 | 59 | 72 |

Suppose the median, or the second quartile $Q_{2}$, is defined as follows:

$$
Q_{2}(n=2 k+1)=(\mathrm{k}+1 \text {-th term }), Q_{2}(n=2 k)=(\mathrm{k} \text {-th term }) \div 2+(\mathrm{k}+1 \text {-th term }) \div 2 .
$$

Therefore, $Q_{2}=Q_{2}(S)=5$-th term $=26$. Now $Q_{1}$ and $Q_{3}$ can be calculated using the methods described there.

## Method 1

| $\mathbf{S}$ | 1 | 1 | 7 | 9 |  | 29 | 52 | 59 | 72 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

$Q_{1}=1 \div 2+7 \div 2=.5+3.5=4, Q_{3}=52 \div 2+59 \div 2=26+29.5=55.5$
Method 2

| $\mathbf{S}$ | 1 | 1 | 7 | 9 | 26 | 29 | 52 | 59 | 72 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

$Q_{1}=7, Q_{3}=52$
Method 3

| $\mathbf{S}$ | 1 | 1 | 7 | 9 | 26 | 29 | 52 | 59 | 72 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

$$
Q_{1}=1 \div 4 \times 3+7 \div 4=2.5, Q_{3}=52 \div 4+59 \div 4 \times 3=229 \div 4=57.25
$$

If $Q_{1}$ is in $[1,7], Q_{2}$ is in [9,29], and $Q_{3}$ is in [52,59], then about $25 \%$ of the values lie at or below $Q_{1}$, about $50 \%$ at or below $Q_{2}$, and about $75 \%$ at or below $Q_{3}$.

