## Answer on Question \#79726 - Math - Differential Equations

Determine the orthogonal trajectory of families. (illustrate)

## Question

1. 

$$
x^{2}+y^{2}+2 a y-1=0
$$

## Solution

Differentiate respect to $x$ :

$$
\begin{gathered}
2 x+2 y y^{\prime}+2 a y^{\prime}=0 \\
x+y^{\prime}(y+a)=0
\end{gathered}
$$

Substitute $y^{\prime}$ to $\left(-1 / y^{\prime}\right)$

$$
\begin{gathered}
x-\frac{(y+a)}{y^{\prime}}=0 \\
y^{\prime}=\frac{(y+a)}{x} \\
\frac{d y}{y+a}=\frac{d x}{x} \\
y+a=c x
\end{gathered}
$$

Answer:

$$
y+a=c x
$$

For example: if $a=0, c=1$

2.

$$
y=a e^{-2 x}
$$

## Solution

$y^{\prime}=-2 a e^{-2 x}$
$\frac{y}{y^{\prime}}=-\frac{1}{2}$
Substitute $y^{\prime}$ to $\left(-1 / y^{\prime}\right)$ :
$y y^{\prime}=\frac{1}{2}$
$2 y d y=d x$
$y^{2}=x+c$
Answer:
$y^{2}=x+c$
For example: if $a=1, c=1$


