

Answer on Question #79309 – Math – Financial Math

Question

You consider buying a business for R600 000. The business is expected to run for 5 years and the following net returns are expected.

- Year 1- R160 000
- Year 2- R250 000
- Year 3- R190 000
- Year 4- R180 000
- Year 5- R130 000

Should you buy the business? A project of this type is expected to return at least 11% per annum. (Show details of your calculation).

Solution

We should buy the business if NPV of this project is greater or equal to 0.

Formula: $NPV = CF_0 + \frac{CF_1}{(1+r)^1} + \frac{CF_2}{(1+r)^2} + \frac{CF_3}{(1+r)^3} + \frac{CF_4}{(1+r)^4} + \frac{CF_5}{(1+r)^5}$, where

- $CF_0 = - 600000$
- $CF_1 = 160 000$
- $CF_2 = 250 000$
- $CF_3 = 190 000$
- $CF_4 = 180 000$
- $CF_5 = 130 000$
- $r = 0.11$ (11%)

The calculation of PV for 5 years is shown in the table below.

Year, (t)	Net Returns CF(t),R	Present Value of annual returns, PV(t),R	Formula for PV in year t (discount rate= r= 11.00%) $PV(t) = \frac{CF(t)}{(1+r)^t}$
1	160000	144144.1441	$PV(1) = \frac{160000}{(1+0.11)^1}$
2	250000	202905.6083	$PV(2) = \frac{250000}{(1+0.11)^2}$
3	190000	138926.3624	$PV(3) = \frac{190000}{(1+0.11)^3}$
4	180000	118571.5753	$PV(4) = \frac{180000}{(1+0.11)^4}$
5	130000	77148.6726	$PV(5) = \frac{130000}{(1+0.11)^5}$
Sum		681696.3629	$PV_{1-5} = \sum_{t=1}^5 PV(t)$

$$NPV = CF_0 + \frac{CF_1}{(1+r)^1} + \frac{CF_2}{(1+r)^2} + \frac{CF_3}{(1+r)^3} + \frac{CF_4}{(1+r)^4} + \frac{CF_5}{(1+r)^5} = -600000 + 681696.36 = 81696.36$$

Answer: Since $NPV=81696.36>0$, we should buy this business.