$$\begin{cases} x = y = z - 1 \\ x^{2}+y^{2}+z^{2}+2(xy+yz+zx)=0 \end{cases}$$
$$\begin{cases} x = y = z - 1 \\ x^{2}+x^{2}+(x+1)^{2}+2(x^{*}x+x^{*}(x+1)+x^{*}(x+1))=0 \end{cases}$$

$$\begin{cases} x = y = z - 1 \\ 9^*x^2 + 6^*x + 1 = 0 \end{cases}$$

 $(3x+1)^2 = 0.$

The system has one solution A(-1/3; -1/3; -4/3).

Thus, Q intersects the cone.

Answer: the statement is false.