## Answer on Question \#77647 - Math - Trigonometry

## Question

A road 9 miles long runs from a point P to a point O on a straight beach, making an angle of $32^{\circ}$ with the beach. Two other straight roads, each 6 miles long, lead from P to the beach. How far is it from O along the beach to the nearer of these?

## Solution


beach

Let X and Y be the ends of the two roads leading to the beach. $\mathrm{PX}=\mathrm{PY}=6$. The question asks to find OX.

Let Z be the middle of XY . Then $\mathrm{OX}=\mathrm{OZ}-\mathrm{ZX}$.
$\mathrm{OZ}=\mathrm{OP} \cos \angle \mathrm{POZ}=9 \cos 32^{\circ}$
$\mathrm{PZ}=\mathrm{OP} \sin \angle \mathrm{POZ}=9 \sin 32^{\circ}, \mathrm{PX}=6=>\mathrm{XZ}^{2}=\mathrm{PX}^{2}-\mathrm{PZ}^{2}=36-81 \sin ^{2} 32^{\circ}$
Then $O X=9 \cos 32^{\circ}-\sqrt{36-81 \sin ^{2} 32^{\circ}}$.
Using calculator $\mathrm{OX}=3.992$ miles.
Answer: 3.992 miles.

