

Answer on Question #77140 – Math – Geometry

Question

A semicircular sheet of metal of diameter 28cm is bent into an open conical cup. What is the approximate depth of the curve?

Solution

$$D = 28\text{cm} \Rightarrow r = \frac{1}{2}D = \frac{1}{2}28 = 14\text{cm}.$$

$$\begin{aligned} \text{Circumference of semicircle} &= \pi * r \Rightarrow \text{circumference of semicircle} = \\ &= \frac{22}{7} * 14 = 44 \text{ cm.} \end{aligned}$$

Circumference of base of cone = circumference of semicircle :

$$\begin{aligned} 2\pi R &= 44 \\ R &= \frac{44}{2\pi} = \frac{44}{2 * \frac{22}{7}} = \frac{44 * 7}{44} = 7\text{cm.} \end{aligned}$$

By the Pythagorean Theorem:

$$(\text{radius of the semicircular sheet})^2 = (\text{depth of the curve})^2 + R^2$$

$$14^2 = (\text{depth of the curve})^2 + 7^2$$

$$196 = (\text{depth of the curve})^2 + 49$$

$$(\text{depth of the curve})^2 = 147$$

$$\text{depth of the curve} = \sqrt{147} = 7\sqrt{3} \approx 12.12\text{cm}$$

Answer: 12.12cm.