

$$\frac{dy}{dt} = -y + 5, \quad y(0) = a$$

$$\frac{dy}{dt} = -y + 5 \Rightarrow \frac{dy}{dt} = -(y - 5) \Rightarrow \frac{dy}{y - 5} = -dt;$$

$$\int \frac{dy}{y - 5} = -\int dt;$$

$$\ln|y - 5| = -t + C,$$

where $C = \text{const.}$

$$\text{So } \ln|y - 5| = -t + C \Rightarrow y - 5 = e^{C-t} \Rightarrow y = 5 + e^{C-t}.$$

$$\text{As } y(0) = a \text{ then } a = 5 + e^{C-0} \Rightarrow C = \ln|a - 5|.$$

Therefore

$$y = 5 + e^{\ln|a-5|-t} = 5 + \frac{a-5}{e^t}$$

$$\text{Answer: } y = 5 + \frac{a-5}{e^t}$$