

Answer on Question #72508, Math / Differential Equations.

Task. $y=2^x \sin(\tan x) \cdot dy/dx$.

Solution.

1) We find $\frac{dy}{dx}$ where $y = 2^x \sin(\tan x)$.

So,

$$\begin{aligned} \frac{dy}{dx} &= (2^x \sin(\tan x))' = (2^x)' \sin(\tan x) + 2^x (\sin(\tan x))' = \\ &= 2^x \ln 2 \sin(\tan x) + 2^x \cos(\tan x) (\tan x)' = 2^x \ln 2 \sin(\tan x) + 2^x \cos(\tan x) \frac{1}{\cos^2 x}. \end{aligned}$$

Answer: $\frac{dy}{dx} = 2^x \ln 2 \sin(\tan x) + 2^x \cos(\tan x) \frac{1}{\cos^2 x}$.

2) We find the general solution of the equation $y = 2^x \sin(\tan x) \frac{dy}{dx}$.

So,

$$\frac{dy}{y} = \frac{dx}{2^x \sin(\tan x)},$$

$$\int \frac{dy}{y} = \int \frac{dx}{2^x \sin(\tan x)},$$

$$\ln y = \int \frac{dx}{2^x \sin(\tan x)},$$

$$y = e^{\int \frac{dx}{2^x \sin(\tan x)}}.$$

Answer: $y = e^{\int \frac{dx}{2^x \sin(\tan x)}}$.