

Answer on Question #71821 – Math – Discrete Mathematics

Question

What are the elements of the set $S = \{x \in (-100, -50) \mid x \equiv 6 \pmod{17}\}$?

Solution

From $x \equiv 6 \pmod{17}$ we can write x as $x = 17t + 6$, where t is integer number. According to the condition of problem $x \in (-100, -50)$. Hence, we obtain the inequality

$$\begin{aligned} -100 < 17t + 6 < -50 &\rightarrow -106 < 17t < -56 \rightarrow -\frac{106}{17} < t < -\frac{56}{17} \\ &\rightarrow -6\frac{4}{17} < t < -3\frac{5}{17}. \end{aligned}$$

Because t is an integer, the solution of inequality $t = \{-6, -5, -4\}$. Therefore x of the set S

$$t = -6 \rightarrow x = -6 \cdot 17 + 6 = -96$$

$$t = -5 \rightarrow x = -5 \cdot 17 + 6 = -79$$

$$t = -4 \rightarrow x = -4 \cdot 17 + 6 = -62$$

$$S = \{-96, -79, -62\}$$

To implement the search on the computer, you must specify a cycle from -100 to -50 in steps of 1 and check the condition for each element $x - 6$ must be divisible by 17. Get the same answer.

Answer: $S = \{-96, -79, -62\}$.