

Answer on Question #71243 – Math – Statistics and Probability

Question

Let t be a random variable giving the number of heads plus the number of tails in three tosses of a coin. List the elements of the sample space S for the three tosses of the coin and assign a value to each sample point.

Solution

The sample space S for the three tosses of the coin is:

$$S = \{HHH, HHT, HTH, HTT, THH, THT, TTH, TTT\}$$

For 3 tosses, possibilities are:

$$HHH: 3 \text{ heads and 0 tails} \Rightarrow t = (\text{heads} + \text{tails}) = 3 + 0 = 3$$

$$HHT: 2 \text{ heads and 1 tail} \Rightarrow t = (\text{heads} + \text{tails}) = 2 + 1 = 3$$

$$HTH: 2 \text{ heads and 1 tail} \Rightarrow t = (\text{heads} + \text{tails}) = 2 + 1 = 3$$

$$HTT: 1 \text{ head and 2 tails} \Rightarrow t = (\text{heads} + \text{tails}) = 1 + 2 = 3$$

$$THH: 2 \text{ heads and 1 tail} \Rightarrow t = (\text{heads} + \text{tails}) = 2 + 1 = 3$$

$$THT: 1 \text{ head and 2 tails} \Rightarrow t = (\text{heads} + \text{tails}) = 1 + 2 = 3$$

$$TTH: 1 \text{ head and 2 tails} \Rightarrow t = (\text{heads} + \text{tails}) = 1 + 2 = 3$$

$$TTT: 0 \text{ heads and 3 tails} \Rightarrow t = (\text{heads} + \text{tails}) = 0 + 3 = 3$$

Sample points	t
HHH	3
HHT	3
HTH	3
HTT	3
THH	3
THT	3
TTH	3
TTT	3

$$\begin{aligned} P(t = 3) &= P(HHH) + P(HHT) + P(HTH) + P(HTT) + P(THH) + P(THT) + \\ &+ P(TTH) + P(TTT) = \\ &= \left(\frac{1}{2}\right)\left(\frac{1}{2}\right)\left(\frac{1}{2}\right) + \left(\frac{1}{2}\right)\left(\frac{1}{2}\right)\left(\frac{1}{2}\right) + \left(\frac{1}{2}\right)\left(\frac{1}{2}\right)\left(\frac{1}{2}\right) + \left(\frac{1}{2}\right)\left(\frac{1}{2}\right)\left(\frac{1}{2}\right) + \left(\frac{1}{2}\right)\left(\frac{1}{2}\right)\left(\frac{1}{2}\right) + \\ &+ \left(\frac{1}{2}\right)\left(\frac{1}{2}\right)\left(\frac{1}{2}\right) + \left(\frac{1}{2}\right)\left(\frac{1}{2}\right)\left(\frac{1}{2}\right) + \left(\frac{1}{2}\right)\left(\frac{1}{2}\right)\left(\frac{1}{2}\right) = 8\left(\frac{1}{8}\right) = 1 \end{aligned}$$