Answer on Question \#70611, Math / Geometry
If the length of both bases and the overall height of an Isosceles Trapezoid are known, is there a formula to determine the interior angles of the shorter base? I know that both angles will be the same. (Need to cut a piece of material with a mitre saw and need to use the saw's angle gauge to make the cut)

Solution


Let $A B C D$ be an Isosceles Trapezoid $(A B=C D)$
We know
$b$ is the length of the larger base $A D$
$a$ is the length of the smaller base $B C$
$h$ is the length of the overall height $B K$
Then
$A K=\frac{A D-B C}{2}=\frac{b-a}{2}$
Consider the right triangle $\triangle A B K$
$\tan (\angle B A K)=\tan \theta=\frac{B K}{A K}=\frac{h}{\frac{b-a}{2}}=\frac{2 h}{b-a}$
Hence
$\angle A B C=180^{\circ}-\angle B A K=180^{\circ}-\arctan \left(\frac{2 h}{b-a}\right)=\angle B C D$
Answer: $\angle A B C=\angle B C D=180^{\circ}-\arctan \left(\frac{2 h}{b-a}\right), \quad b>a$.

