## Answer on Question #69902 – Math – Statistics and Probability

## Question

Free range eggs are produced on a farm. The weights of eggs are found to be normally distributed with a mean of 55g and a standard deviation of 1g. Using the empirical rule and no calculations, determine whether it is likely a randomly chosen egg from the farm would have the following weight.

- **a**. 51g
- **b**. 53g
- **c**. 56g

## Solution

By the empirical rule,

$$P(\mu - \sigma < X < \mu + \sigma) = 0.68,$$
  
 $P(\mu - 2\sigma < X < \mu + 2\sigma) = 0.95,$   
 $P(\mu - 3\sigma < X < \mu + 3\sigma) = 0.997.$   
So

**a.**  $P(X < 51) = P(X < \mu - 4\sigma) < P(X < \mu - 3\sigma) < \frac{1 - 0.997}{2} = 0.0015$  – very unlikely.

**b**. 
$$P(X < 53) = P(X < \mu - 2\sigma) = \frac{1 - 0.95}{2} = 0.025$$
 – unlikely.

**c.** 
$$P(X > 56) = P(X > \mu + \sigma) = \frac{1 - 0.68}{2} = 0.16 - \text{not unlikely.}$$

**Answer: a.** very unlikely; **b.** unlikely; **c.** not unlikely.