

$$4\sqrt{3-4i}$$

$$z = 3 - 4i, x = 3, y = -4, r = \sqrt{x^2 + y^2} = 5, \varphi = \operatorname{arctg}\left(\frac{y}{x}\right) = -\operatorname{arctg}\left(\frac{4}{3}\right)$$

Answer:

$$\begin{aligned} 4\sqrt{3-4i} &= 4\sqrt{z} = 4\sqrt{r} \left(\cos\left(\frac{\varphi + 2\pi k}{2}\right) + i \sin\left(\frac{\varphi + 2\pi k}{2}\right) \right) = \\ &= 4\sqrt{5} \left(\cos\left(\frac{-\operatorname{arctg}\left(\frac{4}{3}\right) + 2\pi k}{2}\right) + i \sin\left(\frac{-\operatorname{arctg}\left(\frac{4}{3}\right) + 2\pi k}{2}\right) \right), k = 0, 1; \end{aligned}$$

$$k = 0 : 4\sqrt{r} \left(\cos\left(\frac{\varphi}{2}\right) + i \sin\left(\frac{\varphi}{2}\right) \right) = 4\sqrt{5} \left(\cos\left(\frac{-\operatorname{arctg}\left(\frac{4}{3}\right)}{2}\right) + i \sin\left(\frac{-\operatorname{arctg}\left(\frac{4}{3}\right)}{2}\right) \right)$$

$$\begin{aligned} k = 1 : 4\sqrt{r} \left(\cos\left(\frac{\varphi + 2\pi}{2}\right) + i \sin\left(\frac{\varphi + 2\pi}{2}\right) \right) = \\ = 4\sqrt{5} \left(\cos\left(\frac{-\operatorname{arctg}\left(\frac{4}{3}\right) + 2\pi}{2}\right) + i \sin\left(\frac{-\operatorname{arctg}\left(\frac{4}{3}\right) + 2\pi}{2}\right) \right) \end{aligned}$$