

Answer on Question #69340 – Math – Algebra

Question

$$f: x \mapsto 3 - 4x - x^2, x < c$$

$$g: x \mapsto \ln(3 - x), x < 3$$

find an expression for $g^{-1}(x)$

Solution

$$g: x \rightarrow \ln(3 - x), x < 3;$$

$$g(x) = \ln(3 - x): D(x) \rightarrow E(g), D(x) = \{x < 3\}.$$

Function $g(x)$ decreases monotonically because

$$g'(x) = \frac{1}{3-x} \cdot (-1) < 0, x < 3.$$

As function $g(x)$, $x < 3$, is monotonous then the inverse function $g^{-1}(x): E(g) \rightarrow D(x)$ exists, where $D(x) = \{x < 3\}$.

Let

$$y = g(x),$$

then

$$e^y = 3 - x,$$

$$x = 3 - e^y.$$

Now switch the x and the y ; the new ' $y = f(x)$ ' will be the inverse function:

$$y = 3 - e^x;$$

Function

$$g^{-1}(x) = 3 - e^x$$

is the inverse of $g(x) = \ln(3 - x)$.

Answer: $g^{-1}(x) = 3 - e^x$.