$$u = ae^{by} + \sin bx$$

Solution.

$$u''_{xy} = b \cos bx + abe^{by}$$