

Answer on Question #67860 – Math – Analytic Geometry

Question

Find a unit vector parallel to the resultant vector $A_1=2i+4j-5k$, $A_2=1+2j+3k$

- a) $\frac{3}{7}i+\frac{6}{7}j-\frac{2}{7}k$
- b) $\frac{1}{7}i+\frac{6}{7}j-\frac{4}{7}k$
- c) $\frac{2}{7}i-\frac{3}{7}j-\frac{5}{7}k$
- d) $\frac{3}{5}i+\frac{6}{5}j-\frac{2}{5}k$

Solution

The resultant vector of $A_1 = 2i + 4j - 5k$ and $A_2 = i + 2j + 3k$ is
 $A = A_1 + A_2 = (2i + 4j - 5k) + (i + 2j + 3k) = (2 + 1)i + (4 + 2)j + (-5 + 3)k = 3i + 6j - 2k$.

Its length is

$$|A| = \sqrt{9 + 36 + 4} = 7.$$

A unit vector parallel to the resultant vector is

$$\frac{A}{|A|} = \frac{3}{7}i + \frac{6}{7}j - \frac{2}{7}k.$$

Answer: a) $\frac{3}{7}i + \frac{6}{7}j - \frac{2}{7}k$.