## Question \#65387, Math / Statistics and Probability

To determine if a single die is balanced or fair, the die was rolled 600 times. The observed frequencies with which each of the six sides of the die turned up are recorded in the following table:
Face 23456
observed frequency 1149284101107102
Is there sufficient evidence to conclude, at the $\% 5$ level of significance, that the die is not fair?

## Answer.

To answer this question we should use Chi-squared test of goodness of fit.

|  | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Expected | 100 | 100 | 100 | 100 | 100 | 100 |
| Observed | 114 | 92 | 84 | 101 | 107 | 102 |

Null hypothesis $H_{0}$ : All faces are uniformly distributed.
Alternative hypothesis $H_{a}$ : All faces are not uniformly distributed.

## Test statistic

$$
\chi^{2}=\sum \frac{\left(o_{i}-E_{i}\right)^{2}}{E_{i}}=\frac{1}{100}\left[14^{2}+8^{2}+16^{2}+1^{2}+7^{2}+2^{2}\right]=5.7
$$

P-value for $\chi^{2}=5.7, d f=5: p=0.3365$.

Since P-value is greater than 0.05 , we can't reject the null hypothesis and should conclude that the die is fair.

