Problem \#6443 In a certain geographic location, $25 \%$ of the wage earners have a college degree and $75 \%$ do not. Of those who have a college degree, $5 \%$ earn more than $\$ 100,000$ a year. Of those who do not have a college degree, $2 \%$ earn more than $\$ 100,000$ a year. If a wage earner is selected at random, find the probability that she or he earns more than $\$ 100,000$ a year.
Solution Let $H_{1}$ - be an event that randomly chosen person has a college degree. $H_{2}$ does not have a college degree. Then $P\left(H_{1}\right)=0.25$ and $P\left(H_{2}\right)=0.75$. Let $A$ be an event that randomly chosen person earns more than $100,000 \$$ a year, then $P\left(A \mid H_{1}\right)=0.05$ and $P\left(A \mid H_{2}\right)=0.02$. Thus, by law of total probability one can get $P(A)=P\left(A \mid H_{1}\right) P\left(H_{1}\right)+$ $P\left(A \mid H_{2}\right) P\left(H_{2}\right)=0.25 \cdot 0.05+0.02 \cdot 0.75=0.0275$.
Answer 0.0275.

