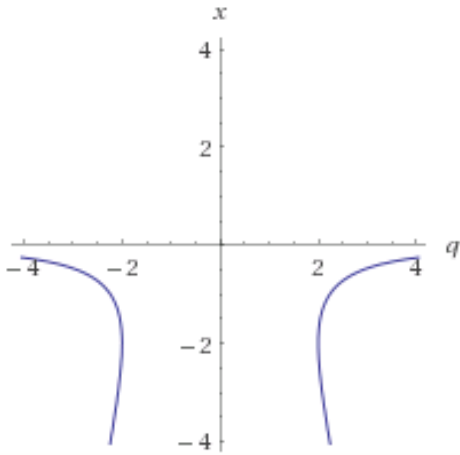


$Q_i = \{q \in \mathbb{N} \mid x^2 + q^2x + 4 = 0 \mid q \text{ is an element of } \mathbb{N}, x \text{ is an element of } \mathbb{R}\}$.

Then:

for $x^2 + q^2x + 4 = 0$:

Implicit plot:



The solution is:

$$D = q^4 - 16$$

$|q| < 2 \Rightarrow$ no solutions ;

$|q| = 2 \Rightarrow x = -2$;

$|q| > 2 \Rightarrow x = 0.5(-q^2 + (q^4 - 16)^{0.5})$; $x = 0.5(-q^2 - (q^4 - 16)^{0.5})$.

Then we can see, that $q = \{2, 3, 4, 5, \dots\}$ (as $q \in \mathbb{N}$), and, respectively, x takes real values. \Rightarrow
 $q = \mathbb{N} \setminus \{1\}$

$$Q_1 = \{2, 3, 4, 5, 6, 7, 8, 9, \dots\}$$

$$Q_2 = \{4, 6, 8, 10, 12, 14, 16, 18, \dots\}$$

...

$$Q_k = \{2k, 3k, 4k, 5k, 6k, 7k, 8k, \dots\}$$

From this we can assume:

$$\bigcup_{i=1}^{\infty} Q_i = Q_1 = \{q \mid x^2 + q^2x + 4 = 0 \mid q \text{ is an element of } \mathbb{N}, x \text{ is an element of } \mathbb{R}\}.$$

$$\bigcap_{i=1}^{\infty} Q_i = \emptyset.$$