## Question

At a party, you and your friend are both eying the last slice of pizza. To settle the matter, you agree on the following dice game: each of you is going to roll a die; if the highest number rolled by either one of you is a 1,2,3 or 4, then Player 1 wins. If the highest number is a 5 or a 6, then Player 2 wins. Assuming that you really want that last slice of pizza would you rather be Player 1 or Player 2 to maximize your chance of winning? Explain your choice.

## Solution

Let's count the total number of cases and in how many ways Player 1 and Player 2 could win the game while rolling two dice.
Since each die has 6 values, we could get $6 \times 6=36$ ways in total.

|  | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $\mathrm{I}(1,1)$ | $\mathrm{I}(1,2)$ | $\mathrm{I}(1,3)$ | $\mathrm{I}(1,4)$ | II $(1,5)$ | II $(1,6)$ |
| 2 | $\mathrm{I}(2,1)$ | $\mathrm{I}(2,2)$ | I $(2,3)$ | I $(2,4)$ | II $(2,5)$ | II $(2,6)$ |
| 3 | $\mathrm{I}(3,1)$ | $\mathrm{I}(3,2)$ | $\mathrm{I}(3,3)$ | $\mathrm{I}(3,4)$ | II $(3,5)$ | II $(3,6)$ |
| 4 | $\mathrm{I}(4,1)$ | $\mathrm{I}(4,2)$ | $\mathrm{I}(4,3)$ | $\mathrm{I}(4,4)$ | II $(4,5)$ | II $(4,6)$ |
| 5 | II $(5,1)$ | II $(5,2)$ | II $(5,3)$ | II $(5,4)$ | II $(5,5)$ | II $(5,6)$ |
| 6 | II $(6,1)$ | II $(6,2)$ | II $(6,3)$ | II $(6,4)$ | II $(6,5)$ | II $(1,1)$ |

The Player 1 wins if two highest numbers rolled is a $1,2,3$, or 4. Thus, we have 16 ways in total.

The Player 2 wins in all other cases, their number is $36-16=20$.

## Answer:

You would rather be Player 2, because person gets more ways of winning than Player 1 (20 against 16), and thus has a better chance of winning.

