

Answer on Question #58325 – Math – Complex Analysis

Question

Let

$$w = \rho(\cos\phi + i\sin\phi),$$

$$z = r(\cos\theta + i\sin\theta)$$

and if n is a positive integer, the n th roots of a complex number are by definition the value of w which satisfies the equation

Solution

The n th roots of a complex number $z = r(\cos\theta + i\sin\theta)$ are defined by

$$w = \sqrt[n]{z},$$

where $w = \rho(\cos\phi + i\sin\phi)$, $\rho = \sqrt[n]{r}$, $\phi = \frac{\theta + 2\pi k}{n}$, $k = 0, 1, \dots, n - 1$.