Answer on Question #57358 - Math - Analytic Geometry

Question

What are the coordinates of the focus of the conic section shown below?

$$y^2 + 16y - 4x + 4 = 0$$

Solution

$$y^2 + 16y - 4x + 4 = 0;$$

 $y^2 + 16y + 64 - 64 - 4x + 4 = 0;$
 $(y+8)^2 = 60 + 4x;$
 $(y+8)^2 = 4(x+15);$
The vertex of the parabola has coordinates $(-15, -8)$.
As $p=1$, it follows that the coordinates of the focus are $(-15+1, -8) = (-14, -8)$.

Answer: (-14, -8).